EYDEL'MAN, M.L., LEMPERT, V.M.

Anticorresion protection of molds made from aluminum alloys.
Tekst. prom. 23 no.7:54-55 Jl '63\* (MIRA 16:8)

1. Nachal'nik proizvodstvenno-tekhnicheskogo otdela Chernovitskogo chulochnogo kombinata (for Eydel'man). 2. Starshiy inahener proizvodstvenno-tekhnicheskogo otdela Chernovitskogo chulochnogo kombinata (for Lempert).

(Textile machinery) (Aluminum-Corrosion)

# "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

#### EYDEL MAN, M.M.

New exhibits at the "Machine Tools and Cutting Tools" section. Inform. biul. VDNKH no.7:5-6 J1 '63. (MIRA 16:8)

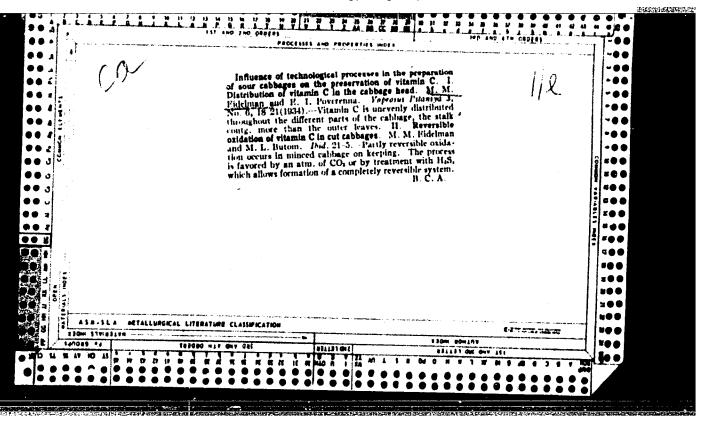
1. Starshiy ekskursovod pavil'ona "Mashinostroyeniye" na Vystavke dostizheniy narodnogo khozoaystva.

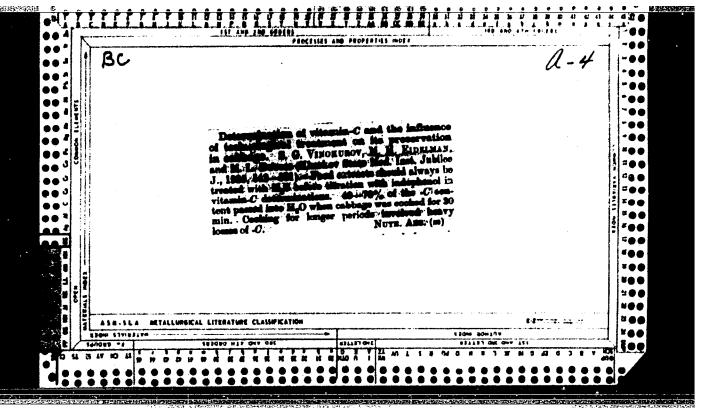
#### "APPROVED FOR RELEASE: Thursday, July 27, 2000

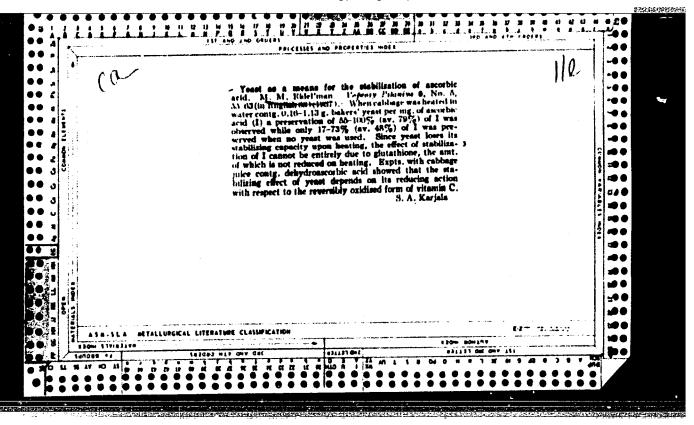
CIA-RDP86-00513R00041231

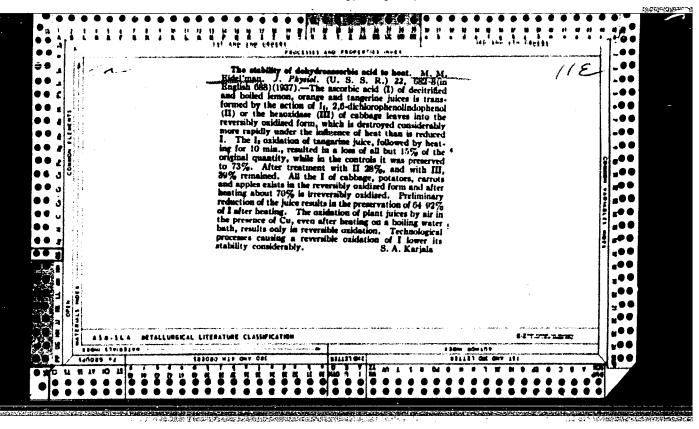
Exhibitions of special stoms. Inform. biul. VINEH no.10:11-33 0 '64 (MRA 18:1)

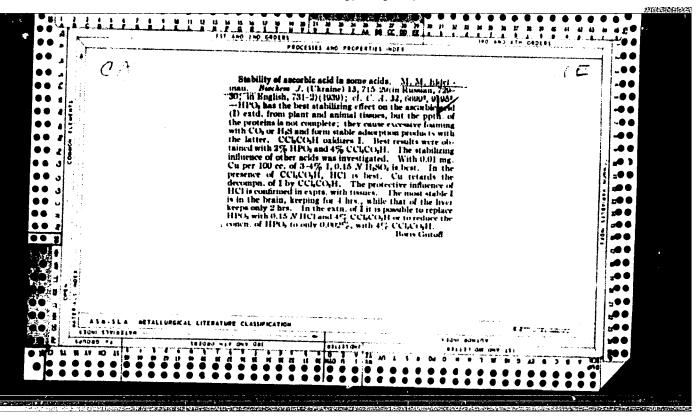
1. Glavnyy metodist po tekstil'noy promyshlemmenti pavil'ena "Legkayn promyshlemment!" (for Deminskaya). 2. Starshiy ekskursoved pavil'ena "Mashinostroyeniye" na Vystavke destizheniy narednogo khozyaystva SSSR (for Eydel'man).

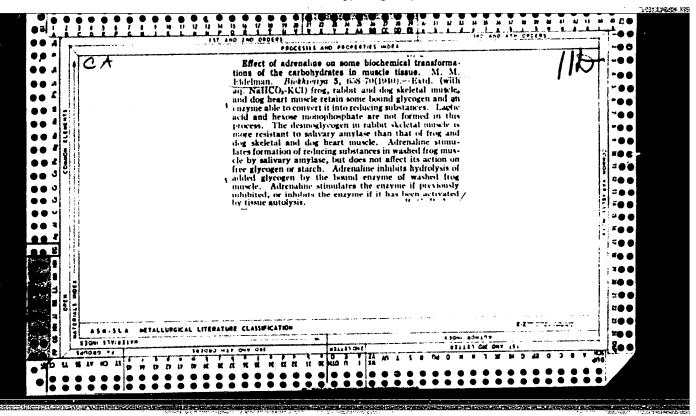


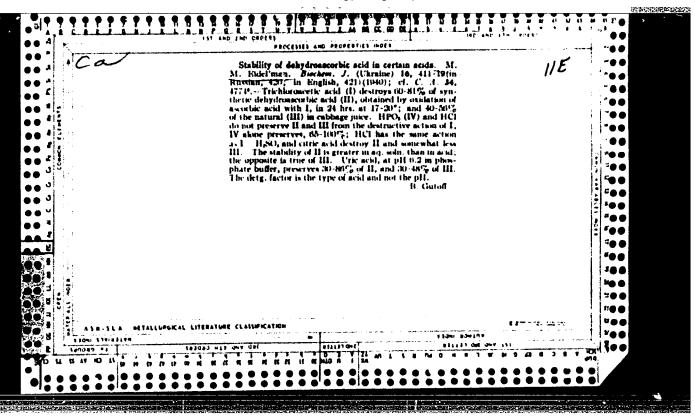


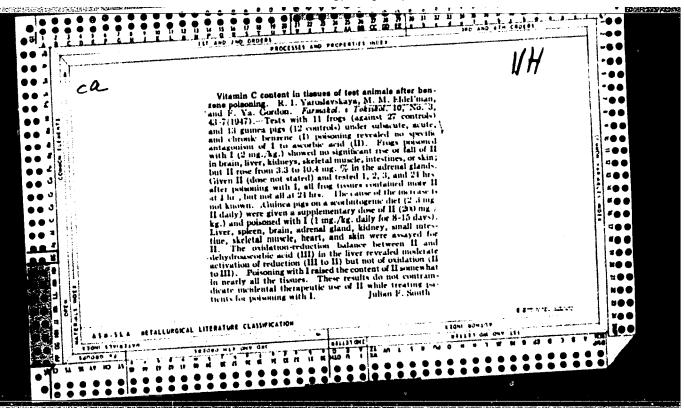


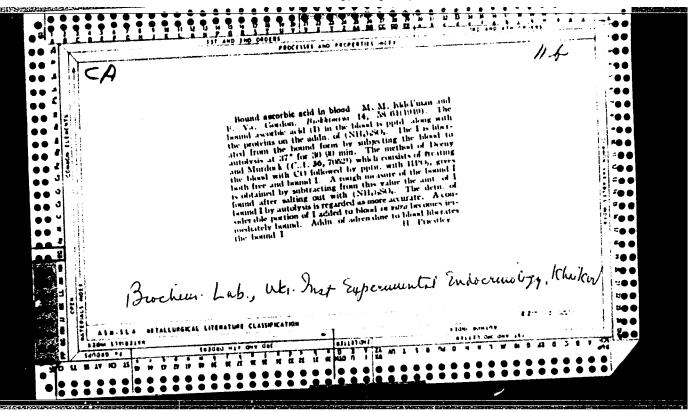


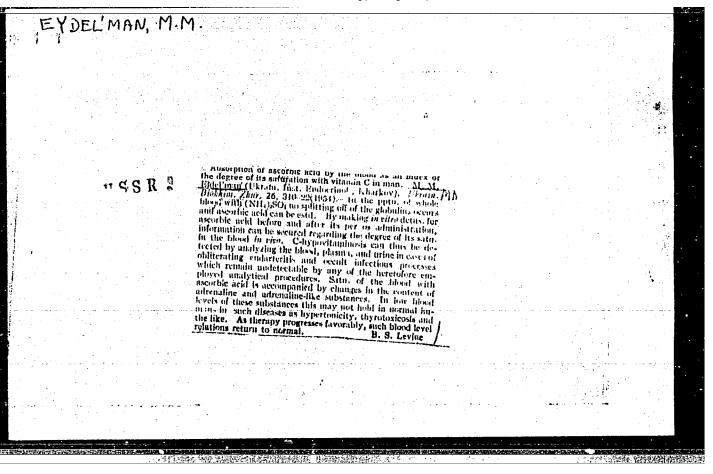










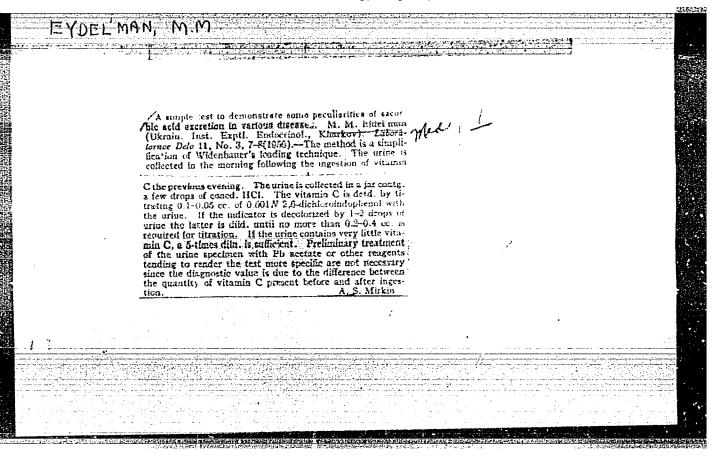


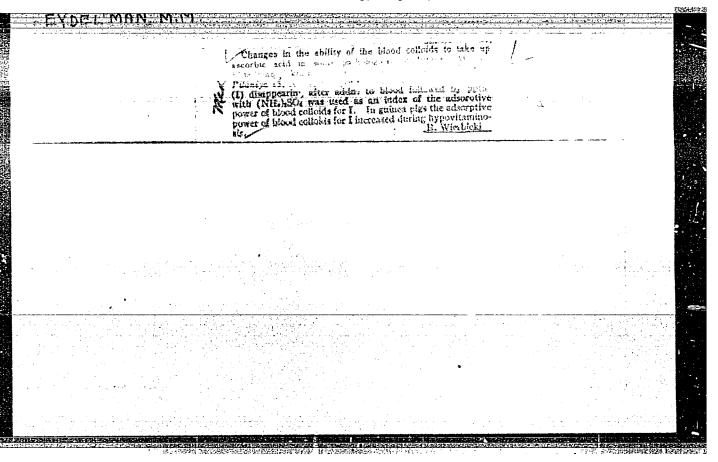
FRUMIN, Z., doktor meditsinskikh nauk (Moskva); ETIEL'MAH, M., kandidat biologicheskikh nauk (Thar'kev).

A new textbook ("The physiology of nutrition." A.M.Breitburg.
Reviewed by Z.Frusin and M.Hidel'man). Sov.torg. no.10:40-41 0

'56. (MLRA 9:12)

(Sutrition) (Breitburg, A.M.)





# EYDEL'MAN, M.M. (Khar'kov) Effect of certain regulatory factors on indicators of adrenalin and ascorbic acid metabolism. [with summary in English]. Probl. (MIRA 11:5) endok. i gorm. 4 no.1:29-45 Ja-F'58 1. Iz otdela biokhimii (sav. - chlen-korrespondent AN USSR prof. A.M. Utevskiy) Ukrainskogo instituta eksperimental'noy endorinologii (dir. - kand.med.nauk S.V. Maksimov) (VITAMIN C, metabolism adrenal cortex, eff. of factors influencing adrenal growth (Rus)) (ADRENAL CORTEX, metabolism vitamin C, eff. of factors influencing adrenal growth (Rus)) EPINEPHRINE, metabolism. eff. of factors influencing adrenal growth (Rus))

EYDELLMAN, M.M., Doo Biol Sci -- (diss) "Goncerning the interaction of adrenalin and ascorbic acid in certain physiological and pathological states of the animal organism." Khartkov, 1997, 26 pp (Khartkov Vet Inst) 300 copies (KL, 36-59, 113)

Study of the regulation of ascorbic acid metabolism. Vitaminy no.4153-59 159. (MIRA 12:9)	
l. Otdel biokhimii Ukrainskogo instituta eksperimental noy endokrinologii, Khar kov. (ASCORBIC ACID)	

UTEVSKIY, A.M.; BARTS, M.P.; BUTOM, M.L.; GAYSINSKAYA, M.Yu.; OSINSKAYA, V.O.;
TSUKERNIK, A.V.; EYDEL'MAN, M.M.

Research on neural regulation of the metabolism of adrenaline and adrenalinelike substances. Sbor. nauch. trud. Ukr. nauch.-issl. inst. eksper. endok. 15:62-72 '99.

(MIKA 14:11)

(ADREMALINE IN THE BODY) (NERVOUS SYSTEM)

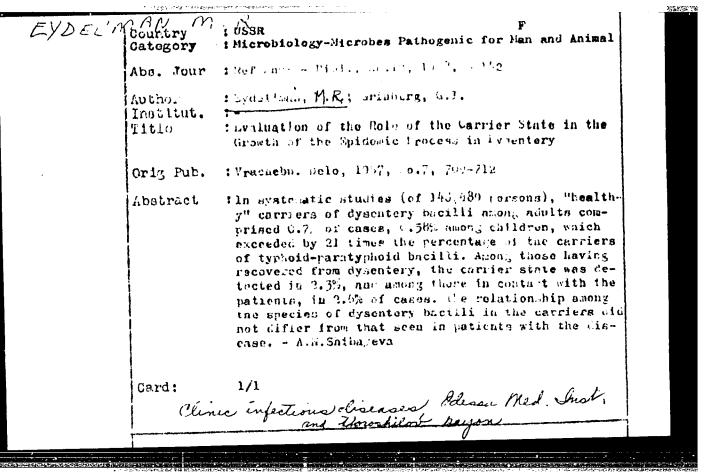
# "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

Bound Ascorbic Acid in the Blood.

report presented at the 5th Int'l.
Biochemistry Congress, Moscow, 10-16 Aug. 1961

Some biochemical indicators of receptive influences of the adrenal glands. Problemok.i gorm. 7 no.2:6-13 '61. (MIRA 14:5) (ADRENAL GLANDS) (ADRENALINE) (ASCORBIC ACID)



THE CONTROLLED PROGRAMMENT AND THE PROGRAMMENT OF T

EYDEL'HAN, H.R., kand.ekon.nauk, red.; USTIYANTS, V.A., red.; KAPRALOVA, A.A., tekhn.red.

[Manual on the divisions of statistics; statistics of population; health; culture; housing and communal economy; budgets of workers, employees and collective farmers; commerce; state purchases; capital construction; automotive transportation; accounting in village soviets] Uchebnoe posobie po otdel'nym otrasliam statistiki; statistika naseleniia, zdravookhraneniia, kul'tury, zhilishchnogo i kommunal'nogo khoziaistva, biudshetov rabochikh, sluzhashchikh i kolkhoznikov, torgovli, zagotovok, kapital'nogo stroitel'stva, avtotransporta i pokhoziaistvennyi uchet v sel'sovetakh. Moskva, Gos.stat.izd-vo, 1958. 406 p. (MIRA 11:5)

EYDEL'MAN, M. R.; GRINFEL'D, A. A.; NIKOLAYEVA, V. L.; MAKAROCHKINA, V. I.; SOTNICHINKO, L. A.

"Data on the healthy carrier of dysentery."

Report submitted at the 13th All-Union Congress of Hygienists, Epidemiologists and Infectionists. 1959

PETROV, A.I., prof.; LESHCHINSKIY, M.I., kand. ekon. nauk; MAKSIMOVA, V.N., dotsent; MALYY, I.G., dotsent; MOSKVIN, P.M., dotsent; TITEL'BAUM, N.P., dotsent; URINSON, M.S., dotsent; EYDEL'MAN, M.R., kand. ekon. nauk; GUREVICH, S.M., red.; GRYAZNOV, V.I., red.; PYATAKOVA, N.D., tekhn. red.

[Course in economic statistics] Kurs ekonomicheskoi statistiki. Izd.3., dop. i perer. Moskva, Gosstatizdat TsSU SSSR, 1961. 507 p. (MIRA 14:6)

(Statistics)

LOKSHIN, E.Yu., doktor ekon. nauk, prof.; ANDREYEVA, O.I., kand. ekon. nauk; VOROSHILOVA, T.S., kand. ekon. nauk, dots.; TARAS'YANTS, R.B., kand. ekon. nauk, dots.; FASOLYAK, N.D., kand. ekon. nauk, dots.; EYDEL!MAN, M.R., kand. ekon. nauk; YAKOBI, A.A., kand. ekon. nauk, dots.; TYAGAY, Ye., red.; MUKHIN, Yu., tekhn. red.

[Economics of the supply of materials and equipment] Ekonomika material'no-tekhnicheskogo snabzheniia; uchebnoe posobie. 2., perer. i dop. izd. Moskva, Gospolitizdat, 1953. 510 p. (Industrial procurement) (MIRA 16:7)

FREYMUNDT, Ye.N., dots.; KORENEVSKAYA, N.N., dots.; IL'CHENKO, S.P.;
SAMOYLOVA, A.A., dots.; GUROV, C.M., dots.; IVANOV, YR.M.;
ZAYTSEVA, N.V., dots.; EYDEL'MAN, M.R., red.; KONIKOV, L.A.,
red.; PONOMAREVA, A.A., tekhn. red.

[Balance of the gross national product of a Union Republic; problems in the theory and methodology of its preparation] Balans obshchestvennogo produkta soiuznoi respubliki; voprosy teorii i metodiki sostavleniia. Moskva, Ekonomizdat, 1962. 326 p. (MIRA 16:4)

1. Moscow. Ekonomiko-statisticheskiy institut. (Gross national product)

EYDEL MAN, M. R.

Statistika material'nogo snabzhemiia / Statistics on the supply of materials / Gosstatizdat, 1953, 224 p.

SO: Monthly List of Russian Accessions, Vol. 7 No. 1 April 1954.

Eydel MAN. M

AUTHOR:

Eydel'man, M.

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2-1-4/9

TITLE:

On the Computation of the Social Product and National Income in the Union Republics (Ob ischislenii obshchestvennogo produkta i natsional nogo dokhoda v soyuznykh respublikakh)

PERIODICAL:

Vestnik Statistiki, 1958, # 1, p 43-55 (USSR)

ABSTRACT:

The article shows how to obtain the indices enabling the statistician to compute the level, structure and production rates of the social product and national income, showing the economical development of every country. It is impossible to project any planning in a socialist economy without analyzing very carefully these indices.

The computation and analysis of these indices are particularly important during the present phase of the USSR economical development. The extended rights of the Union Republics, the changed structure of industrial and construction administration and the establishment of the sownarkhozes demand a higher quality of economical work in the Union Republics and within the district economical administrations.

The methodology of computing the volume of the social product and national income within the Union Republics and the computation of total indices with respect to the whole country,

Card 1/2

2-1-4/9

On the Computation of the Social Product and National Income in the Union Republics

originate from the supposition that the social product and national income are formed by the different branches of material production, such as: industry, construction, agriculture, forestry, freight transport, communication enterprises, trade, public alimentation, material technical supplies, etc.

The author presents four tables showing how to compute some

production figures:

1. The dequence of computational operations of the total volume of material expenses and the production expenses.

2. A general scheme of converting the material expenses

into a joint cost.

3. A computation table showing how to obtain the net value of production from the material gross value of production expenditures.

4. A table for recalculation of costs into prices of 1956.

There are 4 tables.

AVAILABLE: Librar

Library of Congress

Card 2/2

# "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

AUTHOR:

Eydel'man, M.

3CV-2-58-8-6/12

TITLE:

From the History of the National Economy Balance Sheet of the USSR (Iz istorii balansa narodnogo khozyaystva

SSSR)

PERIODICAL:

Vestnik statistiki, 1958, Nr 8, pp 43 - 58 (USSR)

ABSTRACT:

The necessity for compiling a balance sheet of the USSR national economy arises from the planning character of the socialistic society and the law of regular, proportional development of national economy inherent in socialism. The balance of accounts is a system of tables and indices giving an extensive characteristic of socialist reproduction on an enlarged scale. The balance is composed for one year and shows how, during the accounting period, the processes of production, distribution, consumption and accumulation were carried out. It also shows how the correlations and proportions between the individual branches and forms of property were brought about, how the national income was distributed for consumption and accumulation purposes, and how the processes of distribution and redistribution of the social product and national income and

Card 1/3

From the History of the National Economy Balance Sheet of the USSR 6/12

the forming of enterprise profits occurred. The author reviews the balance sheets for 1923, 1928, 1929 and 1930. He then shows how the work on the balance sheets has developed. The article contains a scheme of 14 different sections of the balance sheet. A standard specimen of one of the most important tables (the balance sheet of production, consumption and accumulation of the social production, consumption and accumulation for a good balance sheet is the scientifically developed classification of the branches of national economy and the establishment of exact limits between the productional and non-productional regions. These classifications have been steadily perfected. The author deals with the study of the balance sheet's basic indices, the working out of methods to

Card 2/3

SOV-2-58-8-6/12

From the History of the National Economy Balance Sheet of the USSR

ascertain the share of the individual branches of production in creating the social product and national income.
He emphasizes that the computation of labor expenditure
necessary for production was a complicated task, and outlines the participation of the statistical administrations
of individual Soviet republics in compiling the balance
sheet. In June 1957, a conference of statisticians discussed the question of methodology in compiling the national economy's balance sheet, and worked out a new scheme
of basic tables which replaced the former ones of 1950.
There are 2 tables and 1 Soviet reference.

Card 3/3

SOV/2-59-1-5/10

AUTHOR:

Eydel'man, M.

TITLE:

The Steady Rise in the Prosperity of the Soviet People (Neuklonnyy rost blagosostoya-

niya sovetskogo naroda)

PERIODICAL:

Vestnik statistiki, 1959, Nr 1, p 33 - 48

(USSR)

ABSTRACT:

The author lists the advantages of the socialist type of production for raising the living standard of the population. He refers to the theses of N.S. Khrushchev's report to the 21st KPSS Congress, setting forth a program for a further fast and all-round rise in the living standard during 1959 to 1965. The article contains basic indices on the material welfare of the Soviet people during the forthcoming 7 years covering the national income, number of workmen and employees, industrial production of consumer goods, real wages of workmen and employees, etc. The

Card 1/5

CIA-RDP86-00513R00041231( APPROVED FOR RELEASE: Thursday, July 27, 2000

SOV/2-59-1-5/10

The Steady Rise in the Prosperity of the Soviet People

author examines in detail these basic indices pointing out that in 1958, the national per capita income in the USSR, has increased 15 times as compared with 1913. During the forthcoming 7 years, the national income of the USSR must rise by 62 - 65%. The volume of consumption will increase by 60 to 63%. In 1965, the national income will exceed that of 1913 by 35 to 36 times. A table shows the rate of growth of the USSR national income from 1913 to 1958 as compared with the chief capitalist countries. The article also contains data on the increase in the real wages of workmen and employees, and the real income of farmers. It is pointed out that the regulating of wages of the low and medium paid workmen and employees, which started in recent years, will be continued during the next 7 years. It

Card 2/5

SOV/2-59-1-5/10

The Steady Rise in the Prosperity of the Soviet People

is planned to increase the wages of the lowpaid workmen and employees from 270 - 350 to 500 - 600 rubles per month. The material welfare of the kolkhoz workers and the pension plans are also discussed. In 1966, it is intended to raise the minimum pensions in the cities to 450 - 500 rubles per month. The social insurance fund is composed of contributions from enterprises, administrations and organizations without any deductions from wages. The author deals with state social insurance in case of illness and pregnancy, and with the question of free medical service as important factors of the living standard of the population. One chapter is devoted to the increase in consumption of the most important food products, while the next one deals with the increase in production of articles of the food and light industry by 1965. A table shows the comparative per

Card 3/5

SOV/2-59-1-5/10

The Steady Rise in the Prosperity of the Soviet People

capita figures in the production of milk, butter and meat in the USA and USSR for 1958, the total output of the USSR, the output required to catch up with the USA and the total production in 1965. Some considerations are given to the problem of improving housing conditions. Towards the end of the 7-year plan, housing construction will have increased 1.6 times. Beginning with 1964, a gradual transfer of all workmen and employees to a 30 to 35 hour week is intended. The concluding chapter deals with the rise in the cultural level of the Soviet people. The number of students in schools of general education will increase in 1965 to 38 - 40 million in 1958. Four million other students will be trained in secondary special schools. The total number of specialists with higher education turned out from 1959 to 1965 will

Card 4/5

SOV/2-59-1-5/10

The Steady Rise in the Prosperity of the Soviet People

be 2.3 million against 1.7 million persons from 1952 to 1958. The reorganization of the school system will tend towards a closer contact between training and practical work, and the turning out of fully-educated people. The 7-year plan will establish conditions for a still faster development of all branches of science. There are 6 tables.

Card 5/5

NOVIKOV, V.S., prof., otv.red.; FREYMUNDT, Ye.N., dotsent, zam.otv.red.; RYABUSHKIN, T.V., prof., red.; EYDEL'MAN, M.R., kend.ekon.nauk, red.; MALYY, I.G., dotsent, red.; VASHENTSOVA, V.M., dotsent, red.; ZATTSEVA, N.V., kend.ekon.nauk; SHENTSIS, Ye.M., red.; KAPRALOVA, A.A., tekhn.red.

[Problems in the balance of the economy of a Union Republic; concise stenographic record of an academic conference, January 25-27, 1960] Problemy balansa narodnogo khozisistva soluznoi respubliki; sokrashchennaia stenogramma nauchnoi konferentsii 25-27 ianvaria 1960 g. Moskva, Gosstatizdat, TaSU SSSR, 1960. 118 p. (MIRA 14:3)

- 1. Moscow. Ekonomiko-statisticheskiy institut. 2. Moskovskiy skonomiko-statisticheskiy institut (for Novikov, Freymundt).
- 3. Institut ekonomiki Akademii nauk SSSR (for Ryabushkin).
- 4. TSentral'noye statisticheskoye upravleniye SSSR (for Eydel'man).
- 5. Moskovskiy gosudarstvennyy ekonomicheskiy institut (for Malyy).
  (Russia--Economic policy) (Russia--Statistics)

LOKSHIN, E.Yu., prof., doktor ekon.nauk; ANDREYKVA, O.I., kand.ekon.nauk; VOROSHILOVA, T.S., dotsent, kand.ekon.nauk; TARAS'YANTS, dotsent, kand.ekon.nauk; FASOLYAK, N.D., dotsent, kand.ekon.nauk; EYDEL'MAN, M.R., kand.ekon.nauk; YAKOBI, A.A., dotsent, kand.ekon.nauk; PISKUNOV, V., red.; MUKHIN, Yu., tekhn.red.

[Economics of the supply of materials and equipment; a textbook]
Ekonomika material no-tekhnicheskogo snabzheniia; uchebnoe posobie.
Moskva, Gos.izd-vo polit.lit-ry, 1960. 510 p.

(MIRA 13:11)

(Industrial procurement)

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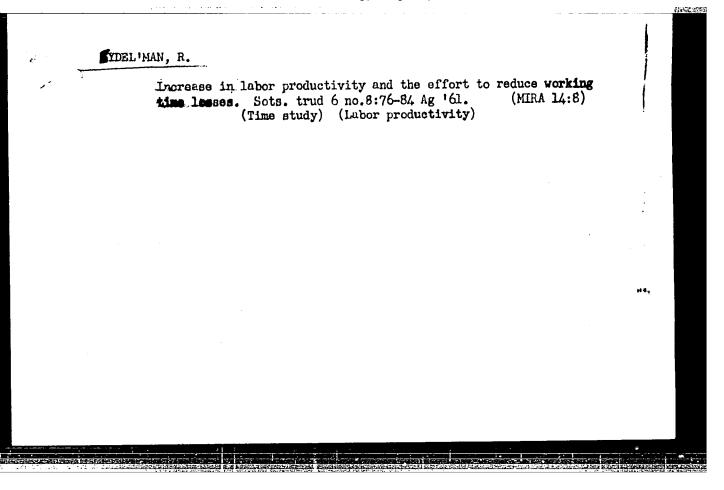
- 1. EYDEL'MAN, M. YA.
- 2. USSR (600)
- 4. Latvia Fur Farming
- 7. Development of collective farm fur farming in the Latvian S.S.R. Kar i zver No. 6 1952.

9. Monthly List of Russian Accessions, Library of Congress, April 1953, Uncl.

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AZERNIKOV, V.; ARLAZOROV, M.; ARSKIY, F.; BAKANOV, S.; LELOUGOV, I.;
BILENKIH, D.; VAMEL', I.; VLADIMIROV, L.; GUGHGEV, G.;
YELAGIN, V.; YERESHKO, F.; ZHURBINA, S.; KAZARNOVSKAYA, G.;
KALIHIH, Yu.; KELER, V.; KONOVALOV, B.; KREYNOLIN, Yu.;
LEBEDEV, L.; PODGORODHIKOV, M.; RABINOVICH, I.; REPIN, L.;
SMOLYAN, G.; TITARENKO, V.; TOPILINA, T.; FEDCHENKO, V.;
ENDEL'NAN, N.; EME, A.; NAUNOV, F.; YAKOVLEV, N.;
MIKHAYLOV, K., nauchn. red.; LIVANOV, A., red.

[Little stories about the great cosmos] Malen'kie rasskazy o bol'shom Kosmose. Izd.2., Moskva, Molodaia gvardiia, 1964.
368 p. (MIRA 18:4)
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#### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231



#### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231

DYACHENKO, V.C.; MAKSIMOV, A.L.; MOSKALENKO, V.K.; SHKURKO, S.I.

The transition of industrial enterprises to a shorter workday in the first five-year plan. Vop.truda no.1:8-66 '58.

(Hours of labor)

LAZUTKIN, Ye.S.; RUSANOV, Ye.S.; EYDEL'MAN, R.A.; TRUENIKOV, S.V.; KAPLAN,
I.I.; ZAGORODNIKOV, M.I.; GOL'TSOV, A.N.; TATARINOVA, N.I.; SONIN,
M.Ya.; SHISHKIN, N.I., doktor geogr.nauk; ANTOSENKOV, Ye.G.;
ZIMYKHOVA, I.I.; KOSYAKOV, P.O.; MATROZOVA, I.I.; ZELENSKIY, G.N.;
SEMENKOV, Ya.S.; ZALKIND, A.I., red.; RUSANOV, Ye.S., red.; SHTEYNER,
A.V., red.; MIKHAL'CHENKO,N.Z.,red.; GERASIMOVA, Ye.S., tekhn. red.

[Manpower of the U.S.S.R.; problems in distribution and utilization]
Trudovye resurey SSSR; problemy raspredeleniia i ispol'zovaniia. Pod
red. N.I.Shishkina. Moskva,Izd-vo ekon.lit-ry, 1961. 243 p. (MIRA 14:12)

Moscow. Nauchno-issledovatel'skiy institut.

(Manpower)

MAMOLAT, A.S.; DVOYRIN, M.S.; ZAMDBORG, L.Ya.; KOVOROTNAYA, N.F.;
EYDEL'MAN, R.I.

Results of the administration of double BCG doses in newborn infants; preliminary communication. Probletub. 39 no.3:16-22 (MIRA 14:5)

1. Iz orgmetotdela (zav. - prof. S.G. Kagan) Ukrainskogo nauchnoissledovatel skogo instituta tuberkuleza (dir. - dotsent A.S. Mamolat) i Chernigorvskogo oblastnogo protivotuberkuleznogo dispansera (glavnyy vrach L.Ya. Zamdborg). (BCG VACCINATION) (INFANTS (NEWBORN))

AKOL'ZIN, P.N.; ARAKEL'YANTS, N.M.; BUYANOVA, O.A.; KIRNOSOV, V.I.;
KISELEVSKIY, S.L.; TARAPIN, V.N.; SHCHEDROVIRSKIY, S.S.;
EYDEL'MAN, R.Ya.

Unified series of strain gauges for the automation of construction and road machinery. Priborostroenie no.8:11-12
Ag '62. (Strain gauges)

Significally, 2. 3.

"Evaluations of the Solutions of Parabolic Systems and Several Applications." Gand Physical Sci, Livov State 9, Livov, 1953. Dissertation (teremailment Example For Sec. 1969)

S.: SEC 186, 19 Aug 1956

EYDEL'MAN, S.D. (Chernovtsy).

Solution estimates for parabolic systems, and some of their applications.

(MIRA 6:9)

(Matrixes) (Differential equations)

EYDELYMAN, S.D.

USSR/Mathematics - Parabolic and elliptic systems

FD-1023

Card 1/1

Pub. 64 3/9

Author

Eydel'man, S. D. (Chernovtsy)

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Title

Relationship among the fundamental matrices of the solutions to

parabolic and elliptic systems

Periodical

Mat. sbor., 35(77), No 1, 57-72, Jul-Aug 1954

Abstract

The author remarks that the fundamental matrix of the solutions for general linear elliptic systems was recently constructed by Y. B. Lopatinskiy in his article "Fundamental system of solutions to an elliptic system of linear differential equations ," Ukr. matem. zhurn., III, No 1 (1951), 3-38. In the present work the author establishes a very simple connection among the fundamental matrices of solutions to parabolic and elliptic systems. This work represents a continuation of the author's "Evaluations of the solutions to parabolic systems and some of their applications," Mat. sbor., 33(75) (1953), 359-382, which contains all the necessary definitions and designations. The relation of the fundamental solutions to the equation of heat conduction and to the Laplace equation with three independent variables has been studied by A. N. Tikhonov ("Equation of heat conduction for several variables," Byull. MGU, sekt-

siya A, I, No 9 (1938), 1-45).

Submitted

4 March 1953

EYDEL MAN, S.D.

USSR/Mathematics - Cauchy's theorem

Card 1/1 : Pub. 22 - 8/4/4

Authors : Eydel'man, S. D.

Title : Cauchy's theorem (problem) for parabolic systems

Pariodical: Dok. AN SSSR 98/6, 913-915, October 21, 1954

Abstract : The article deals with determination of criteria for the values of the

main matrix of the solution of a parabolic system,

 $\frac{\partial u_i}{\partial t} = \sum_{j=1}^{N} \sum_{\sum k_3 \leq 2b} A_{i,j}^{(k_1 k_2 \dots k_n)}(t) \frac{\partial^{k_1 + k_2 + \dots + k_n}}{\partial x_1^{k_1} \partial x_2^{k_2} \dots \partial x_n^{k_n}}$ 

(where i = 1,2,...,N) and for their (values) use for proving the correct applicability (solvability) of Cauchy's theorem (problem) to the class of unlimited functions for parabolic systems with coefficients dependent on both time and space coordinates. Six references (1938-1953).

Institution: Chorovitsy State University

Presented by: Academician I. C. Petrovskiy, June 10, 1954

EYDEL MAN, S.D.

Title

USSR/Matramatics - Liouville's type theorems

Pub. 22 - 4/56 Card 1/1

: Eidel'man, S. D. Authors

WASHINGTON TO THE PARTY OF THE Theorems of Liouville's type theorem for parabolic and elliptical systems

Periodical : Dok. AN SSSR 99/5, 681-684, Dec 11, 1954

: A series of theorems of the Liouville type is proved for the purpose of using Abstract

them as a method for the solution of systems of parabolic and elliptical equa-

tions. Three USSR references (1950-1953).

Institution: The Chernovitsy State University

Presented by: Academician S. L. Sobolev, September 23, 1954.

### CIA-RDP86-00513R00041231 "APPROVED FOR RELEASE: Thursday, July 27, 2000

PG - 3 CARD 1/2 EYDEL'MAN, S.D USSR/MATHEMATICS/Differential equations

SUBJECT

On the analytic behavior of the solutions of parabolic systems. AUTHOR

Doklady Akad. Nauk 103, 27-30 (1955) TITLE PERIODICAL

reviewed 5/1956

By aid of his earlier result on the fundamental matrices of the solutions in the complex domain (Doklady Akad. Nauk 98. No.6 (1954)) the author extends the results of Petrovski (Bull. M.G.U. 1938) to linear parabolic systems

results of Petrovski (2000) 
$$U + A_1(t, x, \frac{\partial}{\partial x}) U = A(t, x, \frac{\partial}{\partial x}) U,$$
(1)  $\frac{\partial U}{\partial t} = A_0(t, x, \frac{\partial}{\partial x}) U + A_1(t, x, \frac{\partial}{\partial x}) U = A(t, x, \frac{\partial}{\partial x}) U,$ 

where the elements of A are differential operators of the order 2b and the elements of  $A_1$  are of order not higher than 2b-1 and the coefficients are analytic functions of the space coordinates. The sketched proofs base on the fact that the fundamental matrix of the system with coefficients depending only on t belongs to the space  $z^q$  defined by Gelfand and Silov (Uspechi mat. Nauk 8, 6 (1953)),  $q = \frac{2b}{100}$ . The principal lemma means that if 1) the

coefficients of (1) are analytic functions of  $x_1$  in a neighborhood  $O_{1}$  of the real point  $t^0, x_1^0, \dots, x_n^0$ ;  $t^0 \le 0$  being complex in  $x_1$  and real in the other variables,

Doklady Akad. Nauk 103, 27-30 (1955)

CARD 2/2 PG - 3

2) the coefficients of the system  $\frac{\partial U}{\partial t} = A_0(t,y,\frac{\partial}{\partial x})U$  are continuous and bounded functions of y,t and have continuous and bounded derivatives relative to  $y_1,\dots,y_n$  up to the order  $r \ge 2b+1$  in the strip  $\bigcap (0 \le t \le T, -\infty < y_8 < \infty)$ , to  $y_1,\dots,y_n$  up to the order  $x \ge 2b+1$  in the strip  $\bigcap (0 \le t \le T, -\infty < y_8 < \infty)$ , to  $y_1,\dots,y_n$  up to the order  $x \ge 2b+1$  in the strip  $\bigcap (0 \le t \le T, -\infty < y_8 < \infty)$ , to  $y_1,\dots,y_n$  up to the order  $x \ge 2b+1$  in the strip  $\bigcap (0 \le t \le T, -\infty < y_8 < \infty)$ , the coefficients possess derivatives of at least first order relative to  $x_1,\dots,x_n$  being continuous and bounded in  $\bigcap$ , then in  $\bigcap$  there exists the fundamental matrix  $Z(t,T,x,\xi)$  which can be continued in the domain  $\bigcap (0 \le t \le T, -\infty)$  being complex in  $y_1$  such that there it is analytic.

By aid of this lemma it can be proved that if the coefficients of (1) satisfy the conditions 1)2)3) of the lemma, then every solution of (1) being regular

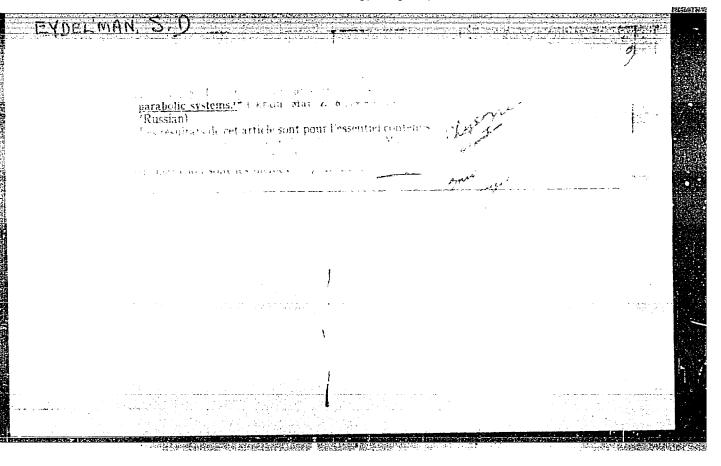
in  $\bigcap$  and belonging to the function class  $|U(x,t)| \leq |x|e^{k|x|^q}$  is an analytic function of  $x_1$ . With a regulary solution the author denotes a solution which is continuous together with its derivatives appearing in the system. For inhomogeneous parabolic systems correspondingly holds: If the coefficients satisfy certain conditions, then every solution satisfying the inhomogeneous system in a certain neighborhood can be continued into the complex such that there it becomes analytic.

INSTITUTION: Public University Cernovizy

# "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231

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Call Nr: AF 11088 Transactions of the Third All-union Mathematical Congress (Cont.) Mo Jun-Jul '56, Trudy '56, V. 1, Sect. Rpts., Izdatel stvo AN SSSR, Moscow, 1956, 23 There is 1 USSR reference.	OBCOW.
Eydel'man, S. D. (L'vov). On the Method of Fundamental Solutions 72.	<b>-</b> 73
There are 4 references, all of them USSR.  74  Section of the Theory of Functions.	-113
Reports of the Following personalities are included:  On Approximation of Function of	<b>1-</b> 75
Many Variables by Entire Panton Many Variables by Entire Panton is made of Dzhrbashyan, M. M.	
Al'per, S. Ya. (Rostov-na-Donu). On the Asymptomatic Values of the Best Approximation of Analytic Function in Complex Region.	5
Card 22/80	
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#### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231



## "APPROVED FOR RELEASE: Thursday, July 27, 2000

PG - 708 CARD 1/2 USSR/MATHEMATICS/Integral equations

SUBJECT EJDEL'MAN S.D. AUTHOR

On an integral equation with an irregular kernel.

Uspechi mat. Nauk 11, 1, 235-239 (1956) TITLE PERIODICAL

reviewed 4/1957

The author considers the integral equation

The author considers the integral equation
$$\frac{t}{(t-\tau)^{3/2}} = \frac{ik^2}{4m(t-\tau)} u(\tau) d\tau, \quad (m>0),$$

from which he seeks a solution by proving at first the lemma 1: If u(t) is a function which admits a continuous derivative of second order and if u(0) = 0, then the operator integral  $A^{(m)}$ , defined by

(2) 
$$\mathbf{A}^{(m)} \mathbf{u} = \frac{1}{2} \int_{0}^{t} \frac{\mathbf{k}}{2\sqrt{\mathbf{m}} (t-\tau)^{3/2}} e^{\frac{i\mathbf{k}^{2}}{4\mathbf{m}(t-\tau)}} \mathbf{u}(\tau) d\tau, \quad (m>0),$$

satisfies the relation:

CARD 2/2

PG - 708

Uspechi mat. Nauk 11, 1, 235-239 (1956)

$$\mathbf{A}^{(m)}\mathbf{A}^{(n)} = \mathbf{A}^{(n)}\mathbf{A}^{(m)} = \frac{1}{2}\mathbf{A}^{\left(\frac{nm}{\sqrt{m}+\sqrt{n}}\right)^{2}}$$

Writing the equation (1) in the form

(3)

(4) 
$$\mu(t) + 2\lambda^{(1)} \mu = \psi(t)$$

and by applying to (4) the iteration method, the author shows that the solution of (1) is given by

Moreover this solution is unique.

## "APPROVED FOR RELEASE: Thursday, July 27, 2000

EYDELMAN, S.D.

CARD 1/2 PG - 399 USSE/HATHEMATICS/Differential equations

SUBJECT

AUTHOR TITLE

The bahavior of the solutions of the heat conducting equation

in the neighborhood of an isolated singularity

PERIODICAL

Uspechi mat., Nauk 11. 3, 207-210 (1956)

reviewed 11/1956

The theorem on the behavior in the neighborhood of an isolated singularity is extended to the solutions of the heat conducting equation:

(1) 
$$\frac{\partial u}{\partial t} = \sum_{k=1}^{m} \frac{\partial^2 u}{\partial x_k^2} .$$

Let  $u(x_1/x_2/x_3/t) = u(x/t)$  be a solution of (1) having an isolated singularity at the origin. We have

$$u(x,t) = \sum_{m=0}^{M-1} \sum_{m_1+m_2+m_3=m}^{2m} a_{m_1}^{m_2} \sum_{m_3}^{2m_3} \frac{\partial^m u(x,t)}{\partial x_1^{m_1} \partial x_2^{m_2} \partial x_3^{m_3}} + u_0(x,t) \quad \text{for } t>0$$

with 
$$U(x,t) = \mathfrak{A}(x,t;0,0)$$
, where the function 
$$\sum_{k=1}^{m} (x_k t; \xi, \tau) = (2\sqrt{\pi(t-\tau)})^{-3} \exp\left[-\frac{1}{4(t-\tau)} \sum_{k=1}^{m} (x_k - \xi_k)^2\right]$$

## "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

Uspechi mat. Nauk 11 3, 207-210 (1956) CARD 2/2 PC . 399

is a fundamental solution of (1). The function u (x,t) is a solution of (1)

being regular at the origin. The number N depends on the order of the

singularity of the function u(x,t). The theorem holds for an arbitrary

singularity of independent variables. The author announces that he has proved

an analogous theorem relative to parabolic systems (in the sense of Petrovskij)

of an arbitrary order in the general form.

EYDEL' MAN, S.D.

SUBJECT

CARD 1/2 PG - 445 USSR/MATHEMATICS/Differential equations

AUTHOR

EIDEL'MAN S.D. On fundamental solutions of parabolic systems.

TITLE Wat. Sbornik, n. Ser. 38, 51-92 (1956) reviewed 12/1956 PERIODICAL

reviewed 12/1956

The principal results of the present investigations have been published in an earlier paper (Doklady Akad. Nauk 97. 913-915 (1954)). The author considers parabolic systems

(1) 
$$\frac{\partial u_{i}}{\partial t} = \sum_{j=1}^{N} \sum_{\sum k_{s} \leq 2b} A_{i,j}^{(k_{1}k_{2}....k_{n})}(t,r) \frac{\partial^{k_{1}+k_{2}+...+k_{n}} u_{j}}{\partial x_{1}^{k_{1}} \partial x_{2}^{k_{2}}....\partial x_{n}^{k_{n}}} \qquad i=1,2,...N$$

or written in matrix form

(2) 
$$\frac{\partial \overline{u}}{\partial t} = P(t, x, \frac{1}{2\pi i} \frac{\partial}{\partial x}) \overline{u}.$$

He constructs the fundamental matrix of the solutions of (2) and investigates

EYDEL'MAN, S.D. EYBEL'MAN, S.D.

SUBJECT

USSR/MATHEMATICS/Differential equations

CARD 1/2 PG - 653

AUTHOR

EIDEL MAN S.D., LIPKO B.Ja.

TITLE

On a theorem of Liouville's type.

PERIODICAL Mat. Sbornik, n. Ser. 40, 273-280 (1956)

reviewed 3/1957

The authors consider the parabolic system

(1) 
$$\frac{\partial \mathbf{U}}{\partial \mathbf{t}} = P_0(\mathbf{t}, \mathbf{x}, \frac{1}{2\pi \mathbf{i}} \frac{\partial}{\partial \mathbf{x}}) \mathbf{U} + P_1(\mathbf{t}, \mathbf{x}, \frac{1}{2\pi \mathbf{i}} \frac{\partial}{\partial \mathbf{x}}) \mathbf{U},$$

where P is a differential operator of order 2b, while the order of the differential operator P1 is at most 2b-1. Besides it is assumed that the derivatives of Green's matrix  $G_0(t, \mathcal{T}, x-\xi, y)$  of the system satisfy certain estimations and that the coefficients of the system in the half space  $t \leq T$ possess continuous and bounded derivatives up to a certain order. By estimation of the fundamental matrix Z(t, T,x, E) constructed by Eidel man (see: Doklady Akad. Nauk 97, 913-915 (1954)) and by aid of some ideas of Gel'fand and Silov (Uspechi mat. Nauk 8, 6, 3-54 (1953)) the authors come to the following assertion: Every solution U(x,t) being regular in  $t \leq T$ of the parabolic system (1), which must satisfy all above mentioned conditions, vanishes identically if for it the inequation

Mat.Sbornik, n.Ser. 40, 273-280 (1956)

CARD 2/2 PG - 653

$$\left| U(x,t) \right| \leqslant \psi(t) e^{\sum_{g=1}^{n} x_g}$$
he function  $\psi(t)$  is contin

is satisfied. The function  $\psi(t)$  is continuous in  $t \le T$  and must still satisfy a condition of increase.

INSTITUTION: Cernovizy.

#### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231

EYDEL'MAN & D.

SUBJECT USSR/MATHEMATICS/Differential equations CARD 1/1 PG - 792

AUTHOR EJDEL'MAN S.D.

TITLE Normal fundamental solution matrices of parabolic systems.

PERIODICAL Doklady Akad. Nauk 110, 523-526 (1956)

reviewed 5/1957

In his earlier investigations on the solvability of the Cauchy problem for the parabolic system

$$\frac{\partial u}{\partial t} = A_0(t,x,\frac{\partial}{\partial x})u + A_1(t,x,\frac{\partial}{\partial x})u \leq A(t,x,\frac{\partial}{\partial x})u$$

the author constructed the normal fundamental solution matrix  $Z(t, \mathcal{T}, x, \xi)$  under the assumption that the coefficients satisfy certain conditions (smoothness, boundedness) in the strip  $\{0 \le t \le T, -\infty < x_8 < \infty\}$  with s=1,2,...,n (Doklady Akad.Nauk 98, 6 (1954); ibid. 103, 1 (1955)). In the present paper the author constructs the solution matrix for a finite region of definition of the coefficients  $\{0 \le t \le T, x \in D\}$ . Under very numerous assumptions he succeeds in constructing a normal fundamental matrix which satisfies sufficient conditions of differentiability and certain estimations. Some similar questions are treated.

INSTITUTION: University Cernovizy.

#### "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

E) DECEMBIL a. D.

SUBJECT

USSR/MATHEMATICS/Differential equations CARD 1/2 PG - 786

AUTHOR

EJDEL'MAN S.D.

TITLE

On regular and parabolic systems of partial differential

equations.

PERIODICAL

the equation

Uspechi mat. Nauk 12, 1 (1957) 254-257

reviewed 5/1957

The paper consists of two sections, one of which in essential was already published (Mat.Sbornik 38, 1,(1956) 51-92 and Doklady Akad.Nauk 110, 4 (1956)). The other section treats systems with coefficients which depend on the time. The consideration of the differential operators in the spaces  $S_{\alpha A}^{\beta B}$  (see Gel'fand and Šilov, Doklady Akad.Nauk 102, 6 (1955)) permits the author, under certain conditions, to prove the uniqueness of the solution of the Cauchy problem for

 $\frac{\partial u}{\partial t} = P(t, \frac{1}{2\pi i} \frac{\partial}{\partial x})u$ 

(uniqueness in the class of functions u(x,t) for which  $|u(x,t)| \le c_2 e^{k|x|}$ ).

The author gives an example for systems being regular in the sense of Gel'fand-Silov, which neither are parabolic nor hyperbolic. For the question of the analyticity of the solutions the following theorem is given: If there exist real  $\sigma_1, \ldots, \sigma_n$  ( $\sigma_1 \neq 0$ ) such that the equation

APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231(

EYDEL MAN, S.D.

20-2-15/62

AUTHOR:

Eydel'man, S.D.

TITLE:

Some Theorems on the Stability of the Solutions of Parabolic Systems (Nekotoryye teoremy ob ustoychivosti resheniy paraboli-

cheskikh sistem)

PERIODICAL:

Doklady Akademii Nauk SSSR, 1957, Vol. 115, Nr 2, pp. 253 - 255 (USSR)

ABSTRACT:

The present paper reports on some theorems concerning the stability (in the sense of Lyapunov) of stable parabolic systems in the sense of I.G. Petrovskiy which are defined in the half space to condense of the solution of (0, T) belong to the class E of the uniqueness of the solution of Cauchy's problem (Koshi's problem). In this connection (0, T) belong to the class E of the uniqueness of the solution of Cauchy's problem (Koshi's problem). In this connection (0, T) distributes a differential operator of the order k with coefficients continuous in the case of (0, T) distributes are obtained by the study of Green's matrix (Grin's matrix) of the above-mentioned system in the half space (0, T) distributes of the thus obtained criteria are direct generalization of the well-known theorem by A.M. Lyapunov for the partial differential equations of the parabolic type. The author here studies the problem of the stability of the trivial solution of this system.

Card 1/2

20-2-15/62

Some Theorems on the Stability of the Solutions of Parabolic Systems

The author gives altogether 2 definitions and 4 rather compre-

hensive theorems. There are 4 Slavic references.

Chernovtsy State University ASSOCIATION:

(Chernovitskiy gosudarstvennyy universitet)

PRESENTED:

February 14, 1957, by I.G. Petrovskiy, Academician

SUBMITTED:

February 12, 1957

AVAILABLE:

Library of Congress

Card 2/2

AUTHOR: EYDEL'MAN, S.D. 20-6-9/42

TITLE: On Cauchy's Problem for Non-Linear and Quasi-Linear Parabolic dynamics of the Company of the Compan

On Cauchy's Problem for Non-Linear and quasi-linear Systems (O zadache Koshi dlya lineynykh i kvazilineynykh parabolicheskikh sistem)

PERIODICAL: Doklady Akad. Nauk, S. S.R. 1957, Vol. 116, Nr 6, pp. 930-932 (USSR)

ABSTRACT: The author considers non-linear systems

 $\frac{\partial \mathbf{u}}{\partial t} = \mathbf{F}(t, \mathbf{x}, \mathbf{u}, \dots, \frac{\mathbf{a}^{2b}\mathbf{u}}{\partial \mathbf{x}_1^{1} \dots \partial \mathbf{x}_n^{n}}) , \text{ quasi-linear systems}$ 

 $\frac{\partial \mathbf{u}}{\partial t} = P_0(t, \mathbf{x}, \mathbf{u}, \dots, \frac{\partial^m \mathbf{n}}{\partial \mathbf{x}_1^1 \dots \partial \mathbf{x}_n^k}, \frac{\partial}{\partial \mathbf{x}})\mathbf{u} + F(t, \mathbf{x}, \mathbf{u}, \dots, \mathbf{x}_n^k)$ 

...,  $\frac{\Im^m_n}{\Im_{x_1}^{k_1} ... \Im_{x_n}^{k_n}}$ ,  $0 \le m \le 2b-1$ ,  $P_0(t,x,y; \frac{\partial}{\partial x})$  a differen-

Card 1/2 tial operator, and systems which differ few from linear systems

20-6-9/42 On Cauchy's Problem for Non-Linear and Quasi-Linear Parabolic 'Systems

$$\frac{\partial u}{\partial t} = P_0(t, x; \frac{\partial}{\partial x})u + F(t, x, u, \dots, \frac{\partial^{2b-1} u}{\partial x_1^2 \dots \partial x_n^n}), \text{ which}$$

altogether are supposed to be parabolic in Petrovski's sense. The correct solubility of Cauchy's problem is investigated. In all the three cases sufficient conditions are given for the existence of a certain correct solution. The proofs are based on the properties of the fundamental solution matrices of linear parabolic systems which recently were investigated by the author [Ref.2]. The present results of the author were already partially announced by him in 1956 on the Third Union Congress of Mathematicians. There are 2 Slavic references.

(Chernovitskiy gosudarstvennyy ASSOCIATION: Chernovtsy State University

universitet)

By I.G.Petrovskiy, Academician, May 15, 1957 May 9, 1957

PRESENTED:

Library of Congress AVAILABLE:

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Card 2/2

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EYDEL'MAN, S. D.: Doc Phys-Math Sci (diss) -- "Investigation of the theory of parabolic systems". Chernovtsy, 1958. 8 pp (Min Higher Educ USSR, Moscow Order of Lenin and Order of Labor Red Banner State y im M. V. Lomonosov), 150 copies (KL, No 5, 1959, 142)

AUTHOR:

Eydel'man, S.D.

SOV/42-13-4-9/11

TITLE:

On a Class of Regular Systems of Partial Differential Equations (Ob odnom klasse regulyarnykh sistem differentsial'nykh uravneniy

v chastnykh proizvodnykh)

Uspekhi matematicheskikh nauk, 1958, Vol 13, Nr 4, pp 205-209 (USSR) PERIODICAL:

ABSTRACT:

It is shown that the system

(1)  $\frac{\partial}{\partial t} \left[ \frac{\partial u}{\partial t} - P(t, \frac{1}{i} \frac{\partial}{\partial x}) u \right] = R(t, \frac{1}{i} \frac{\partial}{\partial x}) u,$ 

where  $\frac{\partial u}{\partial t} - P(t, \frac{1}{i}, \frac{\partial u}{\partial x}) = 0$  is a system parabolic in the sense of Petrovskiy [Ref 4] with M = 2b,  $n_i = 1$  (M - maximal order of

differentiability with respect to  $\mathbf{x}_1, \dots, \mathbf{x}_n$  in the operator P and

2b - parabolic weight) and R is an arbitrary operator with coefficients of at most 2b-th order continuous on [0,T], is neither hyperbolic nor parabolic. At the same time, however, this system (1) is regular in the sense of Gel'fand and Shilov [Ref 1] and therewith it has a certain classical solution. To the class (1) there belongs e.g. the equation for the propagation of sound in

There are 7 Soviet references.

Card 1/2

# "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

On a Class of Regular Systems of Partial Differential SOV/42-13-4-6/11 Equations
SUBMITTED: July 18, 1956

Card 2/2

39-44-4-3/5 Eydel man. S.D. (Chernovtsy)

Liouville Theorems and Stability Theorems for Solutions of AUTHOR: Parabolic Systems (Liuvillevy teoremy i teoremy ob ustoychi-TITLE:

vosti dlya resheniy parabolicheskikh sistem)

Matematicheskiy Sbornik, 1958, Vol 44, Nr 4, pp 481-508 (USSR)

PERIODICAL: (1)The parabolic systems ABSTRACT:

 $\frac{\partial^{n} i_{u_{\underline{i}}}}{\partial t^{n_{\underline{i}}}} = \sum_{j=1}^{N} \sum_{\substack{k_{0} \geq b + \sum k_{s} \leq n_{j} \geq b}} \frac{(k_{0}k_{1} \cdots k_{n})}{A_{\underline{i}} \underline{j}} (t) \frac{\partial^{k_{0} + k_{1} + \cdots + k_{n}} u_{\underline{j}}}{\partial t^{0} \partial x_{1}^{k_{1} \cdots \partial x_{11}}}$ (i = 1, 2, ..., N) $(t \leqslant T \text{ or } t \gg T)$ 

in the sense of Petrovskiy are considered. Several former results of the author [Ref 12,13,14,15] are generalized. § 1. The consideration is based on estimations of Green's matrix  $G(t, \tau, x)$  of (!). It is supposed that it satisfies one of the following conditions for all  $t,\tau,t>\tau$ ,  $x_1,...,x_n$  with

Card 1/4

Liouville Theorems and Stability Theorems for Solutions of 39-44-4-3/5 Parabolic Systems

t>T or t < T:  

$$\Lambda_{1}: \left| \mathbf{p}^{m} \mathbf{G}(\mathbf{t}, \mathbf{T}, \mathbf{x}) \right| \leqslant \mathbf{c}_{m} \left[ \mathbf{a}(\mathbf{t}, \mathbf{T}) \right]^{K_{m}} = -\mathbf{c} \left| \frac{\mathbf{x}}{\mathbf{a}} \right|^{q}$$

$$\Lambda_2: |D^mG(t,T,x)| \leqslant C_m[a(t,T)]^{K_m} e^{-b(t,T) - c\left[\frac{x}{a}\right]^{Q}}$$

where a(t,t), b(t,t) are continuous monotonely increasing functions of t, a(t,t)=0, b(t,t)=0;  $c_{m}$ , positive

constants. The author gives several examples of classes of systems which satisfy the A ...conditions. e.g. strongly parabolic systems, certain systems the coefficients of which are constant or of bounded variation etc. § 2. Four Liouville theorems are proved. e.g.

theorems are proved, e.g. Theorems If for  $t \leq T$  it holds the condition  $\Lambda_1$ , where for

 $T\to -\infty$  it tends  $a(t,T)\to \infty$  and for  $m\to \infty$  it tends  $K_m\to -\infty$ , then each solution of (1) regular in  $t\leqslant T$  satisfying the condition

Card 2/4

Liouville Theorems and Stability Theorems for Solutions of 39-44-4-3/5 Parabolic Systems

 $\left|\frac{3^{k}u_{\frac{1}{2}}}{3t^{k}}\right| \leqslant C\left[i+|x|\right]^{\beta} \qquad (k=0,1,...,n_{\frac{1}{2}}-1)$ consists of a system of polynomials of at most [B] -th degree.

If, however, in (1) it is  $\sum_{s=1}^{n} k_{s} \geqslant 1$  and if B<1, then the

 $u_i$  are constant. Theorems If for  $t \le T$  it holds  $\Lambda_2$  with m = 0 and if a solution of (1) regular in  $t \le T$  satisfies the condition

$$|u(x,t)| \leqslant \varphi(t) e^{k|x|^{M}}$$
,  $1 \leqslant \mu \leqslant q$ 

$$\begin{array}{c} \psi(t_{0})a(t,t_{0}) \stackrel{qn}{q-\mu} + K_{0} \times \underbrace{\mu q}_{cq} \\ \times \exp\left\{-b(t,t_{0}) + a(t,t_{0}) \stackrel{q-\mu}{q-\mu} \left(\underbrace{\mu,\nu k}_{cq}\right) \stackrel{q-\mu}{q-\mu} \right\} \stackrel{q-\mu}{\longrightarrow} 0 \end{array}$$

Card 3/4

### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231

Liouville Theorems and Stability Theorems for Solutions of 39-44-4-3/5 Parabolic Systems

where  $\forall = 1$  for  $\mu = 1$  and  $\forall = 2^{\mu}$  for  $\mu > 1$ , then the solution is identically equal to zero.

In the third paragraph the author shows that the considered properties of the solutions are closely connected with their stability.

Three theorems referring to this are proved. There are 21 references, 18 of which are Soviet, 1 French, and 2 American.

SUBMITTED: November 14, 1956

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Card 4/4

20-120-5-14 67

AUTHOR:

Fundamental Matrices of the Solutions of General Parabolic Systems Eydel'man, S.D. (Fundamental nyye matritsy resheniy obshchikh parabolicheskikh sistem)

ABSTRACT:

TITLE:

PERIODICAL: Doklady Akademii nauk SSSR, 1958, Vol 120, Nr 5, pp 980-983 (USSR) With the aid of the same methods with which the author (in earlier papers [Ref 3,47] constructed and investigated the fundamental metrices of the solutions of linear systems being parabolic in

the sense of Petrovskiy, fundamental solution matrices for

general parabolic systems

general parabolic systems
$$(1) \frac{\partial^{n_1} u_i}{\partial t^{n_1}} = \sum_{\substack{2bk_0 + |k| \leq 2bn_j}} \frac{(k_0 k)}{\lambda_{ij}} (x_i t) \frac{\partial^{k_0}}{\partial t^{k_0}} D_x^k u_j(x_i t)$$

are considered. It is shown that for certain assumptions on the continuity and boundedness of the coefficients of (1) the system (1) possesses a fundamental matrix of solutions which satisfies certain inequalities and which can be continued analytically into the complex domain under further assumptions. The integral operators, the kernels of which are the considered matrices in

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Fundamental Matrices of the Solutions of General Parabolic Systems 20-120-5-14/69

certain L spaces, are explicitly characterized. For an in-

homogenous system obtained from the system (1) by addition of further terms the author investigates the existence and uniqueness

There are 4 references, 3 of which are Soviet and 1 American

ASSOCIATION: Chernovitskiy gosudarstvennyy universitet, (Chernovitskiy State University)

December 9, 1957, by I.G.Petrovskiy, Academician PRESENTED:

SUBMITTED: November 4, 1957

1. Mathematics

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SOV/140-59-2-27/30 16(1)Eydel'man, S.D.

AUTHOR: Integral Maximum Principle for Strongly Parabolic Systems and TITLE

Some of its Applications (Integral'nyy printsip maksimume dlya sil'no parabolicheskikh sistem i nekotoryye yego prilozheniya)

PERIODICAL: Izvestiya vysshikh uchebnykh zavedeniy. Matematika, 1959.

Nr 2, pp 252-258 (USSR)

The author establishes for strongly parabolic systems an integral ABSTRACT:

maximum principle analogous to that of M.M. Lavrent'yev Ref 17

for strongly elliptic systems.

Let u(x,t) be a real regular solution of

 $\frac{\partial \mathbf{u}}{\partial \mathbf{t}} = \sum_{i,j=1}^{n} \frac{\partial}{\partial x_{i}} (\mathbf{A}_{ij}(\mathbf{x},\mathbf{t}) \frac{\partial \mathbf{u}}{\partial x_{j}}) + \sum_{i=1}^{n} \mathbf{B}_{i}(\mathbf{x},\mathbf{t}) \frac{\partial \mathbf{u}}{\partial x_{i}} + \mathbf{C}(\mathbf{x},\mathbf{t}) \mathbf{u}$ 

in the strip  $\prod_i : 0 < t \leq T$ ,  $-\infty < x < \infty$ , and g(x,t) be a

differentiable function of  $x_1, x_2, \dots, x_n$ , t real in  $\prod_{j=1}^n x_j = x_j$ 

Theorem: If  $u(x,t)\in W_{2,g}^{(1)}$ , i.e. if for all  $t_i\in (0,T)$ :

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Integral Marinum Principle for Strongly Parabolic 50V/140-59-2-27/30 Systems and Some of its Applications

$$\|\mathbf{u}(\mathbf{x},\mathbf{t})\|_{\Psi_{2,\mathbf{g}}^{(1)}} \equiv \int_{\mathbf{t}_{+}}^{\mathbf{T}} d\mathbf{t} \left\{ \left\|\mathbf{u}\right\|^{2} + \sum_{i=1}^{n} \left|\frac{\partial \mathbf{u}}{\partial \mathbf{x}_{i}}\right|^{2} \right\} d\mathbf{x} < +\infty,$$

 $|A_{i,j}(x,t)| \leq M$  for  $(x,t) \in \Pi_i$  and if the quadratic form

$$(\mathcal{C}_{c,o}) = \frac{\sum_{i,j=1}^{n} (A_{ij}(x,t)a_{i},a_{j})}{\sum_{i=1}^{n} ((B_{i} + \sum_{j=1}^{n} A_{ij} \frac{\partial g}{\partial x_{i}})a_{i},b)} + ((C - \frac{1}{2} \frac{\partial g}{\partial t} E)b,b) \leq 0$$

for all real vectors  $c = (a_1, ..., a_n, b)$ , then for  $t_1 < t_2$  we have  $F(t_1) \ge F(t_2)$ , where

$$F(t) = ||u(x,t)||_{L_{2,g}} = \int |u|^2 \exp\{-g(x,t)\} dx, |u|^2 = \sum_{g=1}^{N} u_g^2$$

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Integral Maximum Principle for Strongly Parabolic SOV/140-59-2-27/30 Systems and Some of its Applications

If furthermore  $(\mathcal{E}_{c,c}) = \psi(t)(b,b), \psi(t) > 0$ , then

$$F(t_1) \geqslant \exp \left\{-2 \int_{t_1}^{2} \psi(\beta) d\beta \right\} \cdot F(t_2)$$
.

Several conclusions of the theorem are mentioned. There are 4 Soviet references.

ASSOCIATION: Chernovitakiy gosudarstvennyy universitet (Cherno the State University)

SUBMITTED: April 1, 1958

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16(1) AUTHOR:

Eydel'man, S.D.

SOV/20-125-4-14/74

TITLE:

On the Behavior of the Solutions of a Parabolic System in the Neighborhood of an Isolated Singular Point (O povedenii resheniy parabolicheskoy sistemy v okrestnosti izolirovannoy osoboy

PERIODICAL: Doklady Akademii nauk SSSR, 1959, Vol 125, Nr 4, pp 743-745 (USSR)

ABSTRACT:

According to Ya.B.Lopatinskiy  $\int \text{Ref 2} \int a \text{ function } \phi(x) \text{ defined in the finite domain V of the n-dimensional space } x_1, x_2, \dots, x_n$ 

belongs to the functional set  $K_p^0$ ,  $K_{p-0}^0 = \sum_{q < p} K_q^0$  if it is

continuous for  $x \neq x_0$ ,  $x_0 \in V$  and if the expressions

1)  $|\varphi(x)| \cdot |x-x|^p$ , p>0; 2)  $|\varphi(x)|/|\ln|x-x||$ , p=0; 3)  $|\varphi(x)|$ ,

p<0 are bounded. Principal result: In the cylinder G  $\{t_1 \le t \le t_2, x \in V\}$  with the exception of the point  $(x_0,t_0)$  let u(x,t) be a regular solution. of the system

Card 1/3

On the Behavior of the Solutions of a Parabolic SOV/20-125-4-14/74 System in the Neighborhood of an Isolated Singular Point

(1) 
$$\frac{\partial^{m} u}{\partial t^{m}} = \sum_{2bk_{0}+|k| \leq 2bm} A^{(k_{0}k)}(x,t) \frac{\partial^{k_{0}}}{\partial t} D^{k}_{x}u, k_{0} \leq m-1.$$
Let 
$$\int_{t_{1}}^{2} |t-t_{0}|^{1} \left| \frac{\partial^{k_{0}}}{\partial t} D^{k}_{x}u \right| dt \in K_{M+|k|-2b(m+1-k_{0})+n-0};$$

$$2bk_{0}+|k| \leq 2bm-1; 1 = 0, \dots, r; r = \frac{M}{2b}, if \frac{M}{2b} \text{ is integral,}$$

$$r = \left[ \frac{M}{2b} \right]+1 \text{ if } \frac{M}{2b} \text{ is a fraction. Let the coefficients of (1)}$$
be defined in  $G_{1} \left\{ t_{1} \leq t \leq t_{2}; x \in V_{1} \right\}, V \leq V_{1} \text{ and have continuous}$ 
derivatives of the order  $k_{0}^{+}+|k^{-}|$ ;  $2bk_{0}^{+}+|k^{-}| \leq 2b(r-1)+k_{0}+|k^{-}|$  in  $G_{1}$ . If  $r=1$ , then let the derivatives of A with respect to x up to the order  $k_{0}^{+}+|k^{-}|$  be Hölderian. Then it holds

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On the Behavior of the Solutions of a Parabolic System in the Neighborhood of an Isolated

sov/20-125-4-14/74

Singular Point

$$u(x,t) = \begin{cases} \sum_{2bk_0 + |k| \le M-1} \frac{3^{k_0}}{3t_0} \sum_{k=0}^{k} Z(t,t_0,x,x_0) a_{k_0k}(t_0,x_0) + u*(x,t), & t > t_0 \\ k \le M-1 \\ u*(x,t), & t \le t_0 \end{cases}$$

where  $u^*$  is regular in G and  $Z(t,t_0,x,x_0)$  is the fundamental

matrix of the solutions of (1) constructed in \_Ref 4\_.

The author mentions I.G.Petrovskiy, S.V.Kovalevskaya, and E.E.
Levi.

There are 6 Soviet references.

ASSOCIATION: Chernovitskiy gosudarstvennyy universitet (Chernovitsy State

University)

PRESENTED: December 17, 1958, by I.N. Vekua, Academician

SUBMITTED: December 14, 1958

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11

AUTHORS: Eydel'man, S.D., Porper, F.O.

SOV/20-126-5-9/69

TITLE:

On Some Properties of Parabolic Systems in the Sense of G.Ye. Shilov

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PERIODICAL: Doklady Akademii nauk SSSR, 1959, Vol 126, Nr 5, pp 948-950 (USSR)

ABSTRACT:

Let the system

(1) 
$$\frac{\partial u}{\partial t} = \int_{0 \le h \le |k| \le p} A_k(t) D_x^k u$$

be given, where  $|\mathbf{k}| = \mathbf{k}_1 + \mathbf{k}_2 + \dots + \mathbf{k}_n$ ,  $\mathbf{D}_{\mathbf{x}}^k$ 

$$= \frac{\partial |\mathbf{x}|}{\partial \mathbf{x}_{1}^{k_{1}} \partial \mathbf{x}_{2}^{k_{2}} \dots \partial \mathbf{x}_{n}^{k_{n}}}, \mathbf{x} = (\mathbf{x}_{1}, \dots, \mathbf{x}_{n}), \mathbf{u} = (\mathbf{u}_{1}, \dots, \mathbf{u}_{n}),$$

 ${\bf A}_{\bf k}(t)$  is continuous and bounded for t>0. At first the authors consider estimations of the Green natrix of the system. Then these estimations are used in order to investigate the solutions. Two theorems are given. Theorem. 1.) Every solution

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On Some Properties of Parabolic Systems in the Sense of 307/20-126-5-9/69 G.Ye. Shilov

of (1) regular for  $t \le 0$  satisfying the condition

is a system of polynomials of at most  $|u(x,t)| \leq c \left[1 + |x|\right]^{B}$ [B] -th degree in x . 2.) If the  $A_k(t)$  are constants and if a solution regular in  $t \leq 0$  satisfies the condition

 $|u(x,t)| \le C \left[1+|x|\right]^\beta \left[1+|t|\right]^{\frac{1}{2}},$  then this solution is a system of polynomials of at most [B] -th degree in x and of at most the degree

min  $\left\{ \left[ \alpha \right], \left[ \frac{\beta}{h} \right] \right\}$  in t.

I.G. Petrovskiy is mentioned in the paper. The authors thank

G.Ye. Shilov and his followers for valuable discussions.

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On Some Properties of Parabolic Systems in the Sense of G.Ye. Shilov

SOV/20-126-5-9/69

There are 2 Soviet references.

ASSOCIATION: Chernovitskiy gosudarstvennyy universitet

(Chernovtsy State University)

PRESENTED: March 10, 1959, by I.N. Vekua, Academician

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SUBMITTED: March 9, 1959

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#### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231

16(1) AUTHOR:

Eydel'man, S.D.

SOV/20-127-4-8/60

TITLE:

Cauchy Problem for Parabolic Systems With Growing Coefficients

PERIODICAL: Doklady Akademii nauk SSSR, 1959, Vol 127, Nr 4, pp 760-763 (USSR)

ABSTRACT:

The author investigates the correctness of the Cauchy problem for parabolic systems with growing coefficients. The fundamental matrix of the solutions is the up as the sum of the Green's matrix of a shortened system containing only the highest derivatives, and an additional term which is chosen so that the initial system is satisfied. For the Green's matrix there hold the earlier estimations of the author, wherefrom there follows the existence of the sought fundamental matrix and an estimation for it. It is stated that the conditions for the correctness of the Cauchy problem given in [ Ref 1,2 ] are valid also for the considered systems if the growing coefficients do not exceed a certain potential order of increase. The author mentions I.G.

Petrovskiy.

There are 2 Soviet references.

ASSOCIATION: Chernovitskiy gosudarstvennyy universitet (Chernovitsy State

University) April 8, 1959, by I.G.Petrovskiy, Academician

SUBMITTED: April 3, 1959

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PRESENTED:

L 23861-65 EWT(d)/EWA(m)-2 IJP(c)

ACCESSION NR: AR4046313 S/0044/64/000/0

S/0044/64/000/008/B066/B066

SOURCE: Ref. zh. Matematika, Abs. 8B337

AUTHOR: Eydel'man, S. D.; Yangarber, V. A.

TITLE: Some new Liouville theorems on stability for parabolic systems

CITED SOURCE: Nauchn. yezhegodnik za 1958 g. Chernovitsk, un-t. Chernovitsy\*, 1960, 480-483

TOPIC TAGS: parabolic system, Petrov concept, polynomial, square matrix, Green matrix, Liouville theorem, asymptotic stability

TRANSLATION: The parabolic system of the Petrov concept is examined

$$\frac{\partial u}{\partial t} = \sum_{|k| < 10} p_k \left( t, - t \frac{\partial}{\partial x} \right) u = P \left( t, - t \frac{\partial}{\partial x} \right) u, \quad (1)$$

where  $P_k(t,\sigma)$  is a polynomial, with respect to  $\sigma_1,\ldots,\sigma_n$  square matrix of the  $c_{ard}$  1/2

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ACCESSION NR: AR4046313



K degree with continuous and finite coefficients. It is proved that upon satisfying certain conditions on the commutant of system (1) for the Green matrix  $G(t, t_0, x)$  of the system (1), the following estimate is correct:

$$\| G(t, t_0, z) \| < C(t - t_0)^{-\frac{n}{10}} \times$$

$$\times \exp \left\{ - (\sigma - E_0) (t - t_0) - C \left| \frac{z}{(t - t_0)^{\frac{1}{20}}} \right|^{\frac{2b}{2b-1}} \right\}$$

From this the author derives an amplified Liouville theorem and a theorem on asymptotic stability of the solution of system (1) with the help of criteria of asymptotic stability of solutions of the system of usual differential equations developed by Germaidze. O. Red'kina

SUB CODE: MA ENCL: 00

Card 2/2

### "APPROVED FOR RELEASE: Thursday, July 27, 2000 CIA-RDP86-00513R00041231

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SOV/42-15-1-18/27

AUTHOR:

Eydel'man, S. D.

TITLE:

On the Validity of Liouville Theorems for Solutions of Parabolic

Systems

PERIODICAL:

Uspekhi matematicheskikh nauk, 1960, Vol 15, Nr 1, pp 233-234 (USSR)

ABSTRACT:

It is known that the classical Liouville theorem can be extended

from harmonic functions to solution of general parabolic and

elliptic systems (S. D. Eydel'man, Liouville Theorems and Theorems of

Stability for Solutions of Parabolic Systems, Mat. sb. 44 (36): 4 (1958) 481-508) using examples introduced by R. E. Vinograd (On an Assertion of K. P. Persidskiy, U. M. N. Nr 2 (60) (1954)

125-128) in connection with stability problems of ordinary differential equation, the author constructs parabolic systems in the sense of I.G.

Petrovskiy, with variable coefficients such that Liouville's theorem is not valid for the solutions. The examples given are:

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On the Validity of Liouville Theorems for Solutions of Parabolic Systems

$$\frac{\partial u_1}{\partial t} = (\cos 2t - a)(-1)^b \frac{\partial^2 b u_1}{\partial x^{2b}} + (-1 + \sin 2t)(-1)^b \frac{\partial^2 b u_2}{\partial x^{2b}},$$

$$\frac{\partial u_2}{\partial t} = (1 + \sin 2t)(-1)^b \frac{\partial^2 b u_1}{\partial x^{2b}} + (-\cos 2b - a)(-1)^b \frac{\partial^2 b u_2}{\partial x^{2b}}$$
(1)

$$(0 < a \leqslant 1)$$

with solution: 
$$u_1(x, t) = e^{ix + (1-a)t} \cos t$$
,  $u_2(x, t) = e^{ix + (1-a)t} \sin t$ , (2)

limited to a half-plane  $t \leq 0$ .

For parabolic systems: 
$$\frac{\partial v_1}{\partial t} = (-1)^{b-1} \frac{\partial^{1b} v_1}{\partial x^{2b}} + (\cos 2t - a) v_1 + (-1 + \sin 2t) v_2,$$

$$\frac{\partial v_2}{\partial t} = (-1)^{b-1} \frac{\partial^{2b} v_2}{\partial x^{2b}} + (1 + \sin 2t) v_1 + (-\cos 2t - a) v_2,$$
with solution:
$$0 < a < 1,$$

with solution:

$$v_1(x,t) = e^{(1-a)t}\cos t, \quad v_2(x,t) = e^{(1-a)t}\sin t,$$
 (4)

limited to a half-plane  $t \leq 0$ . There are 2 Soviet references.

August 11, 1958

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SUBMITTED:

## "APPROVED FOR RELEASE: Thursday, July 27, 2000

CIA-RDP86-00513R00041231

(1)

16.4.00 77815 807/42-15-1-22**/**27

AUTHOR: Eydel'man, S. D.

Investigations in the Theory of Parabolic Systems TITLE:

(Doctor's Dissertation)

Uspekhi matematicheskikh nauk. 1960, Nr. 1. PERIODICAL:

pp 251-256 (USSR)

ABSTRACT: The dissertation was defended at a session of the

Soviet of the mechanico-mathematical faculty of Moseow University on April 3, 1959. The official opponents were Prof. S. G. Kreyn, Prof. G. E. Shilov. and doctor of the physico-mathematical sciences, E. M. Landis. The thesis is devoted to the investigation of fundamental solution matrices of arbitrary linear parabolic system, in the sense of I. G. Petrovskiv:

 $\frac{\partial^{n_i} u_i}{\partial t^{n_i}} = \sum_{2bh_0 + |h| \leq 2bn_f} A_{ij}^{(h_0 h)}(x, t) \frac{\partial^{h_0}}{\partial t^{h_0}} D^h u_j \qquad (i = 1, 2, \dots, N)$ 

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where

$$D^k = \frac{\partial^{\lfloor k \rfloor}}{\partial x_1^{k_1} \dots \partial x_n^{k_n}}, \quad s^{k_{-2}} s_1^{k_1} \dots s_n^{k_n}, \quad s = 0 \ \ \forall i, \quad z = x + iy, \quad q = \frac{2b}{2b - 1}$$

Estimates of solutions are given and also their application to the investigation of Cauchy's problem for linear and nonlinear parabolic systems, their analyticity, smoothness, stability, and their extension to a neighborhood of singular points. Chapter I deals with the construction of the fundamental solution matrices. It is assumed that the coefficients of (1) depend only on t. Corresponding to (1) the system of ordinary differential equations is studied:

$$\frac{d^{n_{i}}_{u_{i}}}{dt^{n_{i}}} = \sum_{2bk_{0} + |k| \leq 2bn_{j}}^{1} A_{ij}^{(k_{0}k)}(t) (i\sigma)^{k} \frac{d^{h_{0}}_{u_{i}}}{dt^{k_{0}}} \qquad (i = 1, 2, ..., N).$$
 (2)

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Let

$$V(t, \tau, s) = ||v_j^{(t)}(t, \tau, s)||_{i,j=1}^{N}$$

be the matrix whose columns are solutions of (2) with initial conditions:

$$\frac{d^{h_0}v_j^{(t)}}{dt^{k_0}}\bigg|_{t=x} = \delta_{jt}\delta_{h_0n_t-1} \qquad (k_0=0, 1, \ldots, n_j-1, j=1, 2, \ldots, N)$$

where  $\delta$  is the Kroenecker delta. The Fourier transform of V(t,  $\mathcal{T}$  ,s) is the Green's matrix G(t,  $\mathcal{T}$  ,x) of (2):  $G_i^{(t)}(t,\tau,x) = (2\pi)^n \int r^{t(x,\sigma)} V_j^{(t)}(t,\tau,\sigma) d\sigma.$ 

For the Green's matrix of system (1) the following estimate is given:

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$$\begin{vmatrix} \frac{\partial^{h_0}}{\partial t^{h_0}} D_x^h G_s^{(l)}(t, \tau, z) & : C_{h_0 h}(t - \tau)^{\frac{n_j - h_0 - 1 - \frac{(h_l + n)}{2h}}{2h}} \exp\left\{\left(-c \sum_{s=1}^{n} |x_s|^q + \frac{1}{2h-1}\right) + d \sum_{s=1}^{n} |y_s|^q \right\} (t - \tau) \end{vmatrix}^{-\frac{1}{2h-1}}, \quad k_0 = 0, 1, \dots, n_j; |k| = 0, 1, \dots; \\ z_s = x_s + iy_s; \left\{-\infty < x_s < \infty, \ s = 1, 2, \dots, n; \ 0 \ , t < T\right\} \Pi_T,$$
 (3)

where  $c_{k_0k'}$  d are positive constants depending only on

T, c > 0. These estimates permit the construction of fundamental matrices by E. E. Levi's method (S. D. Eydel'man, On Cauch's problem for parabolic systems, DAN 98 Nr 6, 913-915 (1954); S. D. Eydel'man, On Fundamental solutions of parabolic systems, Mat. sb. 38 (80): 1 (1956) 51-92; S. D. Eydel'man, Liouville theorems and stability theorems for solutions of parabolic systems, Mat. sb. 44 (86): 2 (1958) 481-508). These matrices have properties important in applications; i.e., if  $n_1 = n_2 = \ldots - n_N$  then the

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system adjoint to (1) is also parabolic. Chapter 2 Investigates Cauchy's problem for linear and non-linear parabolic systems:

$$\frac{\frac{\partial^{n}(u_{1})}{\partial t^{n_{1}}} = \sum_{j=1}^{N} \sum_{2bk_{0} \in [b(s), 2bn_{j}]} A_{ij}^{(k_{0}k)}(x, t) \frac{\partial^{n}u_{j}}{\partial t^{n_{0}}} D^{k}u_{j} + F_{s}\left(t, u, \dots, \frac{\frac{\partial^{n}u_{j}}{\partial t^{n_{0}}}}{\partial t^{n_{0}}} D^{k'}u_{j}, \dots\right),$$

$$2bk'_{0} + [k'] \leq m_{I} \leq 2bn_{I} - 1,$$
(6)

where  $F_i$  is in general nonlinear. For the system

$$\frac{\frac{\partial^{n_i} u_i}{\partial t^{n_i}}}{\partial t^{n_i}} = F_i \left( t, x, u, \dots, \frac{\frac{\partial^{n_i} u_i}{\partial t^{n_i}}}{\partial t^{n_i}} D^k u_j, \dots \right) \left\{ (i \Rightarrow 1, 2, \dots, N), \quad 2bk_0 + |k| \leqslant 2bu_j \right\}$$
(8)

The Cauchy problem is studied in the class of sufficiently smooth, bounded functions. S. D. Eydel man On Cauchy's problem for linear and nonlinear parabolic systems, DAN 115. Nr 2, 930-932 (1957). Chapter 3 is devoted to the study of properties of regular solutions of

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linear parabolic systems. In appendix 1 of the thesis, S. D. Eydel'man, Integral maximum principle for strongly parabolic systems and some of its applications, Iso. vyssh. ucheb. zaved, Mat., Nr 2 (1959) 252-258, a maximum principle is given for strongly parabolic systems permitting an easy proof of the uniqueness and stability for mixed problems in infinite domains, and the Cauchy problem in the class of rapidly growing functions. The results of the dissertation are given in the following 15 references: S. D. Eydel'man: On Cauchy problem for parabolic systems, DAN 98 Nr 6, (1954), 913-915; Liousville-type theorems for parabelle and elliptic systems, DAN 99 Nr Nr 5 (1954), 681-684; On the analyticity of solutions of parabolic systems, DAN 103 Nr 1 (1955), 27-30; Some theorems on stability of solutions of parabolic systems, DAN 115 Nr 2 (1957), 253-255; On Cauchy's problem for nonlinear and quasilinear parabolic systems, DAN 116 Nr 6 (1957), 930-932; On the behavior of the solution of the heat equation in the neighborhood of a singular point, Usp. Mat. Nauk XI Nr 3 (1956).

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Investigations in the Theory of Parabolic Systems (Doctor's Dissertation)

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207-210; On some properties of solutions of parabolic systems Ukr. mat. journ 8, Nr 2 (1956), 191-207; On fundamental solutions of parabolic systems Matem. sb. 38 (80): 1 (1956), 51-92; On regular and parabolic systems of partial differential equations, Usp. Mat. Nauk Nr 1 (1957), 254-257; On method of fundamental solutions in the theory of parabolic systems, Works III all-union math. conf. Vol 1 (1956), 72-73; Fundamental matrices of solutions of general parabolic systems, DAN 120, Nr 5 (1958), 480-483; On a class of regular systems of partial differential equations, Usp. mat. nauk XIII Nr 4 (1958), 205-209. Integral maximum principle for strongly parabolic systems and some of its applications Tsv. vyssh. ucheb. zaved., Matem Nr 2 (1959), 252-258; On the behavior of solutions of parabolic systems in the neighborhood of a singular point DAN 125, Nr 4 (1959), 743-745; Liouville theorems and stability theorems for solutions of parabolic systems Matem. sb. 44 (86): 2 (1958) 481-508. There are 17 Soviet references.

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